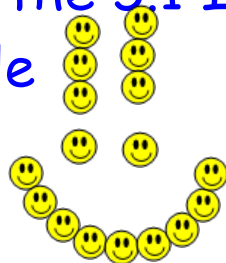


NO clickers OR calculators.

Please get the 5.1 Inverses notes from the brown table



Feb 7-12:21 PM

Algebra 2 Section 5-1

Inverses of Functions

Nov 3-12:34 PM

$f^{-1}(x) = \frac{x-2}{2}$ $f(x) = 2x+9$

Inverse Relation

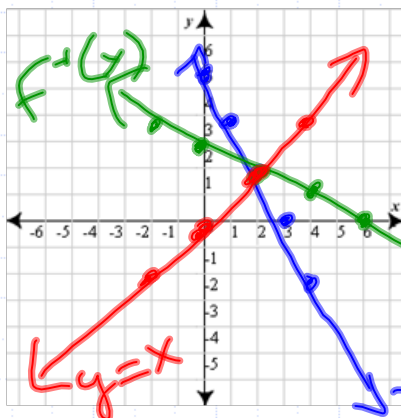
- Given a relation with input and output values, an inverse relation interchanges the input and output values.
 switch
- The domain of the original relation becomes the range of the inverse relation and the range of the original relation becomes the domain of the inverse relation.
- The graph of an inverse relation is a reflection of the graph of the original relation.
- The line of reflection is $y = x$.

∴ Same →

Handwritten notes: $f^{-1}(x) = \frac{x-2}{2}$, $f(x) = 2x+9$, $y = x$, $\frac{-2}{2} = -1$, $\frac{0}{2} = 0$, $\frac{2}{2} = 1$, $\frac{4}{2} = 2$, $\frac{6}{2} = 3$

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Graph the original relation using dots



x	0	1	2	3	4
y	6	4	2	0	-2

x	6	4	2	0	-2
y	0	1	2	3	4

Graph the inverse relation on the same graph using open circles

Now draw in the line $y = x$ and notice the reflection

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Finding inverse relations $y = 2x + 9$

$$x = 2y + 9$$

- To find the inverse relation of a given equation rewrite the equation switching the x and the y
- Now solve the new equation for y
- The resulting equation is the inverse relation

$$x - 9 = 2y$$

$$f(x) = \frac{x - 9}{2}$$

Nov 3-12:34 PM

Inverse Functions

- Functions have inverses also and we find them the same way
- Functions f and g are inverses of each other provided :
 $f(g(x)) = x$ and $g(f(x)) = x$
Substitute one function for x in the other function
- We often write the inverse of function f using the notation f^{-1}

Verify that $f(x) = 3x - 5$ and $g(x) = \frac{1}{3}x + \frac{5}{3}$ are inverse

Show: that $f(f^{-1}(x)) = x$.

$$f(g(x)) = 3 \left(\frac{1}{3}x + \frac{5}{3} \right) - 5$$

$$x + 5 - 5$$

$$g(f(x)) = \frac{1}{3}(3x - 5) + \frac{5}{3}$$

$$x - \frac{5}{3} + \frac{5}{3}$$

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Find an equation for the inverse of the relation
 $y = 3x - 5$.

↩ Rewrite original relation
 Solve for y.

$$x = 3y - 5$$

$$\frac{x+5}{3} = \frac{3y}{3} \quad \frac{x+5}{3} + \frac{5}{3} = y$$

Find an equation for the inverse of the relation
 $y = \frac{1}{2}x + 4$.

$$x = \frac{1}{2}y + 4$$

$$2(x-4) = \left(\frac{1}{2}y\right) \cdot 2$$

$$2(x-4) = y$$

$$f^{-1}(x) = 2x - 8$$

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Fitness

Elastic bands can be used in exercising to provide a range of resistance. A band's resistance R (in pounds) can be modeled by $R = \frac{3}{8}L - 5$ where L is the total length of the stretched band (in inches).

• **Do NOT Switch** Find the inverse of the model (Solve for L).

$$\frac{8}{3}(R+5) = \left(\frac{3}{8}L\right) \frac{8}{3} \quad L = \frac{8}{3}(R+5)$$

• Use the inverse function to find the length at which the band provides 19 pounds of resistance.

$$L = \frac{8}{3}(19+5)$$

$$L = \frac{8}{3} \cdot 24 = 3 \cdot 8$$

$$L = 64 \text{ in}$$

Nov 3-12:34 PM

GUIDED PRACTICE

Find the inverse of the given function.

1. $f(x) = x + 4$

2. $f(x) = 2x - 1$

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Pg. 175-176
1-19
Pick 12

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