

$x^2 + 3x - 7$

**Algebra 2 3-9 Graphing Factorable Polynomial Functions**

**Objectives:**

- 1) Find all possible rational zeros of a polynomial function
- 2) Graph the polynomial function
- 3) Find all the actual rational zeros
- 4) Factor a polynomial completely

*Factored form*

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Graphing Polynomial Functions – Ex 1

- Graph  $f(x) = (x - 2)(x + 1)(x + 3)$

**Degree: 3**  
**ODD**

\* **odd exponent** the graph will go through the x-axis  
 \* **even exponent** the graph will touch (bounce back) the x-axis

- What are the zeros of the graph?  
 $x = 2$   $x = -1$   $x = -3$
- Does that relate to the equation in any way?

*Max: (-2.12, 4.06)*  
*Min: (2.12, -8.21)*

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Graphing Polynomial Functions – Ex 2

- Graph  $f(x) = (x + 2)^2(x - 4)$

**Degree: 3**

- What are the zeros of the graph?  
 $x = -2$   $x = 4$
- Does that relate to the equation in any way?

*Min: (2, -32)*

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No clickers & yes calculators.

Have out the 3.9 notes and find the zeros for the next equation.

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Graphing Polynomial Functions – Ex 3

- Graph  $f(x) = (x-1)^2(x+2)(x-3)$

Even/Odd = 4  
 Pos/Neg L.C. = Positive  
 # of Zeros: 3

BB  
 • What are the zeros of the graph?  
 $x=1, x=-2, x=3$   
 • Does that relate to the equation in any way?

min @ (4, -5.17)  
 min @ (1.5, -16.3)

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Relationships between the graph and the equation

SKIP

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Using the graph to factor – Ex 1

- Graph  $f(x) = x^3 - 7x + 6$

Even/Odd: odd  
 Pos/Neg L.C.: Positive  
 # of Zeros: 3

• What are the zeros?  
 $x = -3, x = 1, x = 2$   
 Do Any Zeros BB? No

• How do they look if we put them back in the parentheses?  
 Factored form:  
 $f(x) = (x+3)(x-1)(x-2)$

Max: (-1.53, 13.1)  
 Min: (1.53, -1.13)

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Using the graph to factor – Ex 2

Standard Eqn: LARGEST Exponent

- Graph  $f(x) = 2x^3 + 3x^2 - 1$

Even/Odd: odd  
 Pos/Neg L.C.: Positive  
 # of Zeros: 2

• What are the zeros?  
 $x = -1, x = 0.5$   
 Do Any Zeros BB? yes

• How do they look if we put them back in the parentheses?  
 Factored form  
 $f(x) = (x+1)^2(x-.5)$  Add the Exponents

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### Rational Zero Test

- If a rational number  $\frac{r}{s}$  (written in lowest terms) is a zero of the polynomial function  $f(x) = a_n x^n + \dots + a_1 x + a_0$  where the coefficients  $a_n, \dots, a_1$  are integers with  $a_n \neq 0$  and  $a_0 \neq 0$ , then  $r$  is a factor of the constant term  $a_0$  and  $s$  is a factor of the leading coefficient  $a_n$ . **SKIP**

You can make a list of all the possible factors by identifying all the possible combinations of  $\frac{r}{s}$  **most factors possible up to that factors**

\*Remember – factors can be positive or negative

$x^3 + 7x + 1$

3 factors  
 $(x+1)^2(x-1)(x+5)$   
 4 factors

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### Example 1

- Find the rational zeros of  $f(x) = 2x^3 - 7x^2 + 2x + 3$
- r values:
- s values:
- List all the possible rational zeros:
- Use a calculator to graph the function.
- Identify the actual zeros of the function
- Write the function in factored form.

$x = -5, x = 1, x = 3$

$f(x) = (x+5)(x-1)(x-3)$

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### Example 2

- Find the rational zeros of  $f(x) = x^3 - x^2 - 8x + 12$
- r values:
- s values:
- List all the possible rational zeros:
- Use a calculator to graph the function.
- Identify the actual zeros of the function.
- Write the function in factored form.

$x = -3, x = 2$

$f(x) = (x+3)(x-2)^2$

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Zeros  
 Max  
 mins

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## Practice 1

- Find the rational zeros of  $f(x) = 2x^3 - 7x^2 - 10x + 24$
- r values:
- s values:
- List all the possible rational zeros:
  
- Use a calculator to graph the function.
- Identify the actual zeros of the function.
- Write the function in factored form.



## Practice 2

- Find the rational zeros of  $f(x) = x^4 + 2x^3 - 8x^2 - 18x - 9$
- r values:
- s values:
- List all the possible rational zeros:
  
- Use a calculator to graph the function.
- Identify the actual zeros of the function.
- Write the function in factored form.



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